

EXPLAIN LENGTH OF LAY

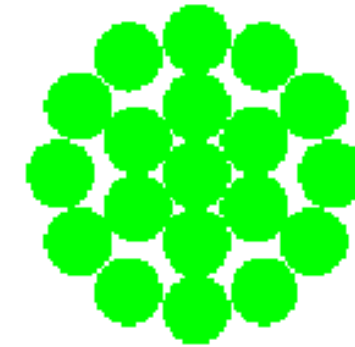
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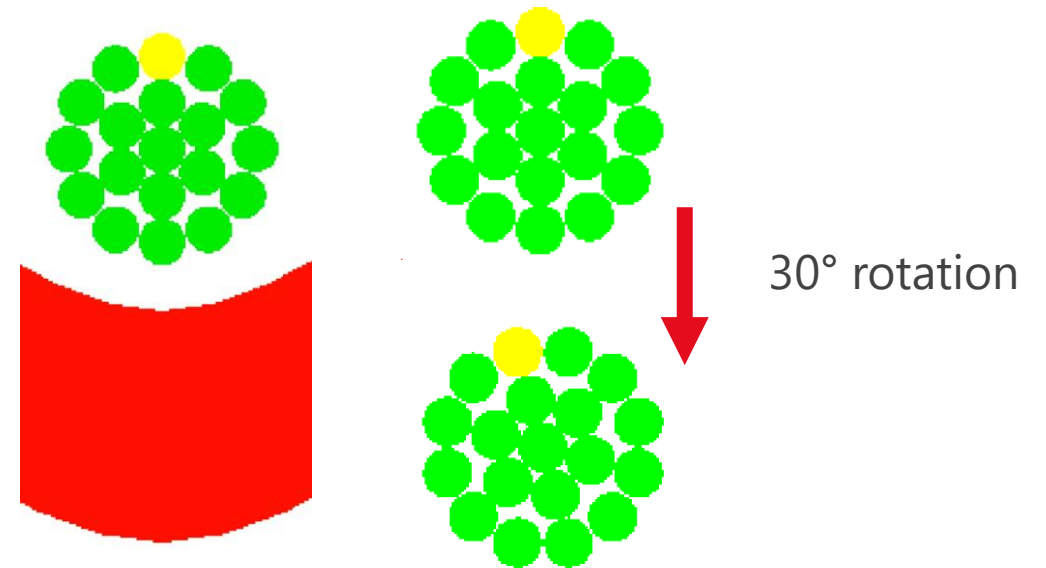
- The length of lay gives the distance that is needed for the thread to perform a full 360° rotation around itself (twist).
- The structure in **Weave**Geo is always generated periodically.
 - This means a thread leaving on one side of a unit cell re-enters it on the other side.
 - This holds also for a structure composed of multiple unit cells
- In general, the size of a unit cell must be a multiple of the length of lay.
 - This ensures that the thread makes an integer number of 360° rotations.
- Depending on the thread type, this condition can be weakened.
 - As a special case we show this for the 1x19 rope.

SPECIAL CASE: 1X19 ROPE

- The 19 filaments are arranged in a circular packing.
 - The outer circle contains 12 filaments.
 - The middle circle contains 6 filaments.
 - The last filament is in the center.
- For the outer circle after a rotation of $360^\circ/12=30^\circ$ every thread is on the position of another thread (see pictures on the right).
- For the middle circle this is the case after a rotation of $360^\circ/6=60^\circ$.
- The minimal possible rotation for this kind of thread is the least common multiple of 30° and 60° which is 60° .
- The maximum length of lay (distance needed for a full rotation) is $6 * l_u$, where l_u is the length of the unit cell.



Arrangement of the filaments in a 1x19 rope



- In **WeaveGeo**, the factor how much of the rotation can be performed in the unit cell is determined by rounding $y = \frac{6 \cdot l_u}{\text{length of lay}}$ to the next integer z .
 - This gives the number of 60° rotations.
- For the maximal length of lay we get $y = 1$.
- Smaller values for length of lay are possible.
 - In fact, the algorithm changes the length of lay, such that it fits to the computed integer value.
 - This ensures that the periodicity is maintained.
- The corrected length of lay is computed with the formula: corrected length of lay = $\frac{1}{\left(\frac{z}{6 \cdot l_u}\right)}$.

SPECIAL CASE: 1X19 ROPE

- If the entered length of lay is more than two times the maximal length of lay we get

$$y < \frac{6 \cdot l_u}{2 \cdot 6 \cdot l_u} = 0.5. \text{ This is rounded down to } z = 0.$$

- This means no twist is performed.
- For the corrected length of lay we get: $\frac{1}{\left(\frac{0}{6 \cdot l_u}\right)} = \frac{1}{0} = \text{inf}$.
- This leads to the warning shown below.
 - We will improve this message.

